

**S2.2-18:**  $10 \times 9 \times 8 \times 7 = 5040$ ;

(a).  $9 \times 9 \times 8 \times 7 = 4536$ ;

(b).  $5040 - 1 \times 1 \times 8 \times 7 = 4984$ .

**S2.3-12:** (a).  $\frac{11!}{4!4!2!} = 34,650$ ;

(b) Treating all P's as one entity, the answer is  $\frac{10!}{4!4!} = 6300$ ;

(c) Treating all I's as one entity, the answer is  $\frac{8!}{4!2!} = 840$ .

(d) Treating all P's as one entity, and all I's as another entity, the answer is  $\frac{7!}{4!} = 210$ .

(e). By (a) and (c), The answer is  $840/34650 = 0.024$ .

**S2.4-18:**  $\binom{6}{2}5^4/6^6$ .

**S2.4-30:** (a)

$$\frac{\binom{2}{1}\binom{98}{49} + \binom{2}{2}\binom{98}{48}}{\binom{100}{50}}.$$

(b).  $2^{50}/\binom{100}{50}$ .

**R2-22:**

$$\frac{\binom{15}{1}\binom{15}{1}\binom{14}{1}\binom{14}{1}\cdots\binom{1}{1}\binom{1}{1}}{\binom{30}{2}\binom{28}{2}\cdots\binom{4}{2}\binom{2}{2}} = \frac{(15!)^2}{30!/(2!)^{15}}.$$

**R2-24.** An ordinary deck of 52 cards is dealt, 13 each, at random among A, B, C, and D. What is the probability that (a) A and B together get two aces; (b) A gets all the face cards; (c) A gets five hearts and B gets the remaining eight hearts?

**Sol:** (a).  $\frac{\binom{4}{2}\binom{48}{24}}{\binom{52}{26}}$ . (b).  $\frac{\binom{12}{12}\binom{40}{1}}{\binom{52}{13}}$ . (c).  $\frac{\binom{13}{5}\binom{39}{8}\binom{8}{8}\binom{31}{5}}{\binom{52}{13}\binom{39}{13}}$ .