Autonomous Navigation of Wireless Robot Swarms with Covert Leaders

Xiaofeng Han° Louis F. Rossi* Chien-Chung Shen°

Abstract—The integration of advanced computation, wireless communication, and control technologies has facilitated the creation of autonomous robot swarms for many civil and military applications. In nature, animals that travel in groups often rely on social interactions among group members to make movement decisions. In many cases, few individuals within the group have pertinent knowledge about the destination and/or migration routes. In this paper, we adapt a swarm model developed for animal groups to study the unique problems associated with covert leadership in the context of wireless robot swarms. We term this problem autonomous navigation with covert leaders. In this covert leadership problem, only a small subset of robots in a robot swarm possess extra information that guides their movement, and both this information and the identities of those individuals possessing this information remain covert (to minimize the chance of being compromised). We describe a distributed navigation algorithm, where each robot locally makes its movement decision solely based on one-hop information collected via wireless communications. The effectiveness and merits of the described navigation algorithm are demonstrated through extensive simulations.

Index Terms—Robot Swarms, Navigation, Covert Leaders.

I. INTRODUCTION

Animals that travel in groups often rely on social interactions among group members to make movement decisions. In many cases, few individuals within the group have pertinent knowledge about the destination and/or migration routes. Based on such observation, Couzin et al. [1] has developed a swarm model showing how information can be transferred within animal groups both without explicit signaling and when group members do not know which individuals possess such knowledge.

The integration of advanced computation, wireless communication, and control technologies has facilitated the creation of autonomous robot swarms for many civil and military applications, where groups of robots running swarm algorithms self-organize to achieve different goals. A swarm algorithm is loosely defined as a set of rules which a group of robots follow to interact locally with other proximal robots without any centralized control. In particular, certain sets of rules in certain swarm algorithms self-organize the group into coherent, useful structures and behavior such as a uniformly translating mass traveling in a fixed direction, or a milling mass which holds a fixed position.

In this paper, we adapt the swarm model described in [1] to study the unique problems associated with covert leadership in the context of wireless robot swarms. We term this problem autonomous navigation with covert leaders. Covert leadership in a wireless robot swarm involves long-standing problems associated with swarm algorithms and introduces new problems and challenges unique to wireless communications that do not exist in biological contexts. In typical leadership problems in swarms, a small subset of individuals possess extra information that guides their movement. For security concerns, both this information and the identities of those individuals possessing this information are covert. Furthermore, it is critical that this information not be broadcast via wireless communications and it is best to have the covert information on as few robots as possible (to minimize the chance of being compromised). The key differences are wireless definitions of robot proximity, decision making data arriving at discrete intervals, and covert leadership as a desirable quality. All swarm algorithms rely upon the notion of proximal interactions, but proximity in most biological systems is defined through direct sensory input e.g., visual contact. In contrast, proximity associated with wireless communications is determined by transmission power, channel fading, path loss, among other factors. The second difference is that decision making data in biological systems arrive continuously in time or essentially continuously since nervous system respond on a time scale faster than the motion of the individual in most cases, whereas data arrives in discrete bursts in a wireless system. The last difference is that we consider a unique scenario where the information possessed by leaders is absolutely covert in contrast to biological systems where it is possible and in some cases likely that leaders can be identified through sensory or behavioral cues.

Swarm techniques have been developed to control robots, such as pattern formation [2], [3] and navigation [4]. However, these swarm solutions either do not utilize wireless communications as the coordination methods or assumes that robots can continuously exchange information without any communication collision or packet loss. As pointed in [5], the usage of wireless communications in networked control systems poses new challenges on the optimization of performance in the face of constraints on communication bandwidth, congestion, and contention for communication resources, delay, jitter, noise, fading, and the management of signal transmission power. Furthermore, most existing work on autonomous navigation focuses on computing trajectories satisfying certain constraints, such as collision-free or obstacle avoidance, for each individual.
robot. For instance, the trajectories can be computed globally assuming that the working environment is completely known [6], or computed locally by each robot using information collected in real-time in dynamic environment [7], [8]. However, these efforts assume that the pertinent information related to routes and destinations is known to all the robots. In addition, these efforts do not use wireless communications as the coordination method among robots.

Our solution is very different from existing work on autonomous navigation in that we apply covert leadership to control the movement of wireless robot swarms. Our algorithm aims to navigate a robot swarm from one location to another while satisfying the follow requirements: (1) the number of leaders should be as small as possible, (2) the leaders’ identities should remain covert, and (3) the destination information should remain secret. The proposed navigation algorithm is fully distributed, and each robot executes the algorithm asynchronously using information collected via wireless communications from one-hop neighbors.

The remainder of the paper is organized as follows. Section II briefly reviews the navigation model presented [1] for animal groups. Section III presents our navigation algorithm for wireless robot swarms. Performance of the presented algorithm is evaluated via extensive simulations in Section IV. Section V concludes the paper with future research directions.

II. BASIC SWARM MODEL

This section briefly reviews the navigation model for animal groups as described in [1]. The perceptual field of each animal is divided into zone of repulsion (ZOR), zone of orientation (ZOO) and zone of attraction (ZOA), as shown in Fig. 1. Given a distribution of \( N \) animals, to coordinate with the neighbors in different zones, animal \( i \) (located at position vector \( P_i \) and pointing in direction \( D_i \)) will move away from the neighbors in ZOR or move along with the neighbor in ZOO while moving towards the neighbors in ZOA, and therefore will have three decision vectors,

\[
DR_i = \sum_{j \in S_{ZOR}} \frac{R_{ij}}{|R_{ij}|}, \\
DO_i = \sum_{j \in S_{ZOO}} \frac{D_j}{|D_j|}, \\
DA_i = \sum_{j \in S_{ZOA}} \frac{R_{ij}}{|R_{ij}|},
\]

where \( R_{ij} = P_i - P_j \) is a displacement vector between the \( i^{th} \) and \( j^{th} \) animal, and \( S_{ZOR}, S_{ZOO} \) and \( S_{ZOA} \) are the sets of indices of animals in the zones of repulsion, orientation and attraction, respectively. Similarly, \( |S_Z| \) denotes the number of elements in zone \( Z \). The normalization of the decision vectors is not discussed in [1], but we assume that each decision is treated as a unit vector in the network simulations.

If we assume that decision vectors are normalized as unit vectors then the biologically inspired swarming algorithm introduced in [1] is as follows.

1) If \(|S_{ZOR}| \neq 0 \) then \( V_i = DR_i \), Break.
2) If \(|S_{ZOO}| \neq 0 \) and \(|S_{ZOA}| = 0 \) then \( V_i = DO_i/|DO_i| \), Break.
3) If \(|S_{ZOO}| = 0 \) and \(|S_{ZOA}| \neq 0 \) then \( V_i = DA_i/|DA_i| \), Break.
4) If \(|S_{ZOO}| \neq 0 \) and \(|S_{ZOA}| \neq 0 \) then \( V_i = \alpha \times DO_i/|DO_i| + (1 - \alpha) \times DA_i/|DA_i| \).

It is important to note that other normalizations are possible and some are more effective than others in producing self-organized, coherent behavior. Typically, \( \alpha \) is chosen to be 1/2. Enhancements of the basic model include limited cones of perception and limited turning rates. Another interesting feature of this basic swarming algorithm is that the decision vectors are spatially discontinuous. This means that slight changes in relative positions may cause the direction vector to change abruptly responding to animals crossing zone boundaries. This is not a major issue in biological applications where the size of the zone of repulsion is relatively small. In mobile networking applications one desires well-spaced network to achieve maximal coverage. In fact, a desired zone of repulsion can be as much as 30% of the transmission radius. In simple discontinuous models like these, high swarm densities lead to unstable behavior and no self-organization will occur.

In leadership studies, there are two types of animals, leaders and non-leaders. Leaders possess extra information about the environment. In our study, the leaders possess a vector \( F_i = P_d - P_i \) pointing to the desired destination, where \( P_d \) is the position vector of destination. Leaders will set their new orientation to be

\[
D_i = \beta \times V_i + (1 - \beta) \times F_i.
\]

where typically \( \beta \) is chosen to be 1/2. Non-leaders will set their new orientation to be

\[
D_i = V_i.
\]

While only a small fraction of the animals possess destination information, the swarming rules effectively communicate this information to non-leaders through the rule-based dynamics of the swarm. Under proper conditions, the leaders will guide non-leader neighbors toward a consensus direction through covert leadership. Note that each animal, either leader or non-leader, will keep observing its proximity and continuously use
the coordination rules to interact with the neighbors within different zones. Simulation results in [1] indicate that a small percentage leaders can effectively lead the group to the destination point.

III. DISTRIBUTED NAVIGATION ALGORITHM FOR WIRELESS ROBOT SWARMS

Although the navigation model described in [1] effectively mimics the covert leadership behavior existing in animal groups, this model cannot be directly applied to wireless robot swarms due to the constraints imposed by wireless communications. We therefore present a distributed and asynchronous autonomous navigation algorithm designed specifically for wireless robot swarms.

A. System Model of Wireless Robot Swarms

The system model of wireless robot swarms makes the following assumptions.

Assumption 1: A wireless robot swarm is composed of ‘homogeneous’ robots, where each robot executes the same swarm algorithm and possesses identical omni-directional wireless communication capability.

Assumption 2: Since the one-hop propagation delay in wireless communications is usually very low (in the order of milliseconds), the propagation delay is ignored such that each broadcast packet can be received immediately after its transmission.

Assumption 3: Each robot is aware of its own position at all time. Such position information can be obtained via GPS or other localization algorithms. The position of the destination is known only to a small set of covert leaders within the robot swarm.

Assumption 4: Each robot moves at the same speed $V$ and can turn its moving direction to any direction it desires. However, the model is readily to be extended to the situations where robots move at different speed or have limited maximum turning angle.

B. Distributed Autonomous Navigation Algorithm

Adopting the idea of [1], the transmission area of each robot (viewed as a circle centered at the robot with radius being equal to the transmission radius) is divided into zone of repulsion, zone of orientation, and zone of attraction, respectively. However, to facilitate interactions between ‘neighboring’ robots using these three zones, we need to address the following two critical issues. First, characteristics of wireless communications make it impossible for a robot to continuously receive the position information from all of its neighbors. Robots can only exchange information periodically. Second, potential collisions of wireless communications make it impossible for a robot to receive the position information from all of its neighbors at the exact same time. As a result, when a robot needs to decide its moving direction according to the coordination rules, it must be able to estimate the current positions and moving directions of its neighbors based on previously received information.

To address these issues, each robot independently divides the time into time slots of fixed length. At the beginning of a new time slot, based on the information collected in the previous time slot, each robot calculates its moving direction according to the coordination rules and immediately broadcasts a hello packet containing its current position and new moving direction. Then each robot will move along the decided direction until the next time slot. How the time slots help each robot to estimate the updated information about its neighbors is depicted in Figure 2. Each robot, say $R_i$, maintains a neighbor cache, which is reset to empty at the beginning of each time slot. During a particular time slot starting at time $T_1$, upon $R_i$’s receiving a hello packet from robot $R_j$ at local time $T_j$, $R_i$ records the position $P_{j1}$ and the moving direction $D_{j}$ of $R_j$ together with timestamp $T_j$ in its neighbor cache. Using the information in the neighbor cache, $R_i$ can estimate the new position $P_{j2}$ of $R_j$ at the beginning of $R_i$’s next time slot, i.e., $T_j + T_{\text{interval}}$, using Equation 4, since $R_j$ is assumed to move along $D_j$ at speed $V$ until $T_j + T_{\text{interval}}$, which is later than $T_1 + T_{\text{interval}}$.

$$P_{j2} = P_{j1} + (T_1 + T_{\text{interval}} - T_j) \times \frac{D_j}{|D_j|} \times V$$

Algorithm 1 presents the autonomous navigation algorithm, and the notations used in the algorithm are listed in Table I. Notice that Algorithm 1 is an event-driven algorithm, and each robot executes this algorithm independently until the entire swarm arrives at the destination. Moreover, since the algorithm only employs the local time of each robot, there is no need to synchronize the entire swarm.

![Diagram](image-url)
Algorithm 1: Autonomous Navigation Algorithm

1: **OUTPUT:** Robot $R_i$ periodically computes its moving direction $D_i$;

2: **START UP**
3: $R_i$ waits for a random time $T_{j0}$ between $[0, T_{jitter}]$.
4: if ($R_i$ is a leader robot) then
5: Set $D_i$ to be the direction $\frac{P_A - P_i}{|P_A - P_i|}$ towards the destination;
6: else
7: Set $D_i$ to be a random direction;
8: end if
9: $R_i$ broadcasts a hello packet containing its position $P_i$ and moving direction $D_i$;
10: $R_i$ resets its neighbor cache, schedules a timer for next time slot starting at $T_{i1} = T_{i0} + T_{interval}$, and starts moving along $D_i$;
11: **END START UP**

12: **UPON EVENT** Receive hello packet from $R_j$ at $T_{ij}$;
13: $R_i$ records the position $P_j$ and moving direction $D_j$ of $R_j$ together with time stamp $T_{ij}$ in its neighbor cache;
14: **END UPON EVENT**

15: **UPON EVENT** Timer ticks for new time slot at $T_{in}$:
16: $D_i = DR_i = DO_i = DA_i = null$;
17: for each record $R_j$ in the neighbor cache do
18: $R_i$ computes the distance $|R_iR_j|$;
19: if ($|R_iR_j| \leq R_{zor}$) then
20: $DR_i = DR_i + \frac{P_i - P_j}{|P_i - P_j|}$;
21: end if
22: if ($R_{zor} < |R_iR_j| < R_{zoo}$) then
23: $DO_i = DO_i + \frac{P_i - P_j}{|P_i - P_j|}$;
24: end if
25: if ($R_{zoo} < |R_iR_j| < R_{zoa}$) then
26: $DA_i = DA_i + \frac{P_i - P_j}{|P_i - P_j|}$;
27: end if
28: end for
29: if ($NR \neq null$) then
30: $D_i = \frac{NR_i}{|NR_i|}$;
31: else
32: $D_i = \alpha \times \frac{R_{zor}}{|R_{zor}|} + (1 - \alpha) \times \frac{R_{zoo}}{|R_{zoo}|}$;
33: if ($R_i$ is a leader robot) then
34: $D_i = \beta \times \frac{P_i - P_j}{|P_i - P_j|}$;
35: end if
36: end if
37: $R_i$ broadcasts a hello packet containing its position $P_i$ and moving direction $D_i$;
38: $R_i$ resets neighbor cache, schedules a timer for next time slot starting at $T_{in+1} = T_{in} + T_{interval}$, and starts moving along $D_i$;
39: **END UPON EVENT**

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**Table II**

**Simulation Configurations**

| PHYSICAL and MAC Layer Protocols | 802.11b |
| Data Rate (MBPS) | 5 |
| Transmission Range (Meters) | 354 |
| Broadcast Interval (Seconds) | 2 |
| Initial Jitter (Seconds) | 1 |
| Number of Robots | 10 - 50 |
| Speed (MPS, Meters / second) | 1 - 10 |
| Percentage of Leaders (%) | 10 - 25 |

| $\alpha$ | 0.5 |
| $\beta$ | 0.5 |

IV. SIMULATION STUDY

We conduct extensive simulation to evaluate the performance of the proposed autonomous navigation algorithm with respect to two evaluation metrics, average arrival ratio and average arrival time, whose formal definitions are given below. In the simulation, the initial robot swarms are randomly deployed with a density of 50 robots per square kilometer. We use QualNet as the simulation platform. Table II summarizes the configurations of these simulations. All of the qualitative results presented in this section are the average of 100 trials.

**Definition 4.1:** [Successful Arrival]: A robot swarm successfully arrives at the destination if the swarm is connected and the destination point is within the transmission area of at least one robot leader.

**Definition 4.2:** [Average Arrival Ratio]: For a robot swarm using a given configuration and moving to the destination, its average arrival ratio is the number of successful arrivals over the number of total simulation runs.

**Definition 4.3:** [Average Arrival Time]: For a robot swarm using a given configuration and moving to the destination, the average arrival time is the average time that the swarm needs to arrive at the destination point over all of the successful arrivals.

A. Evaluation of the Size of the Three Zones

In the first set of simulations, we set the moving speed of each robot to be 5 MPS, and let a wireless robot swarm containing 30 robots with 15% leaders move to a destination point about 5 kilometers away. We repeat this simulation with different configurations of $R_{zor}$, $R_{zoo}$ and $R_{zoa}$.

Figures 3(a), 3(b) and 3(c) demonstrate the navigation process of the robot swarm using $R_{zor} = 40$ meters, $R_{zoo} = 274$ meters and $R_{zoa} = 40$ meters. It takes about 1180 seconds for the swarm to get to the destination. Once arriving at the destination, the entire swarm will move around the destination point, as shown in 3(c).

Figures 4(a) and 4(b) compare the performance of the robot swarm using different combinations of $R_{zor}$, $R_{zoo}$ and $R_{zoa}$ (We increase $R_{zor}$ and $R_{zoa}$ from 0% to 10% of the transmission radius, respectively). First, when the sizes of $R_{zor}$ and $R_{zoa}$ are less than 10% of the total transmission range (area 1 in figure 4(a)), which implies a large $R_{zoo}$ about 80% of the transmission range, the robot swarms can quickly move to the destination with 100% average arrival ratio. Second, as shown in area 2 in figure 4(a), for $R_{zor}$
ranging from 0% to 20% of the transmission range, there is a valid range of $R_{ZOA}$ ranging from 5% to 70% of the transmission range, within which the robot swarms can arrive at the destination with arrival ratio 100%. Also, when the size of $R_{ZOR}$ increases, the valid range of $R_{ZOA}$ decreases correspondingly. Third, when $R_{ZOR}$ is larger than 22.5% of the transmission radius, the robot swarms fail to arrive at the destination most of the times. However, exceptions occur when $R_{ZOR}$ is between 50% and 80% of the transmission range, where the robot swarms can actually arrive at the destination with high average arrival ratio by choosing a small $R_{ZOA}$. Such results deserve more explanation. We track the movement of the swarms and find that when $R_{ZOR}$ is within this particular range, with small $R_{ZOO}$ and $R_{ZOA}$, the robot swarms can still adjust to consensus moving directions towards the destination and hence eventually arrive at the destination. However, after successfully arriving at the destination, if no further action is taken, only leader robots may stay, while non-leader robots will continue moving and result in partition. Finally, we also notice that when the average arrival ratio decreases, the average arrival time increases correspondingly.

B. Evaluation of the Number of Robots

We then evaluate how the number of robots in the swarms would affect the performance of our navigation algorithm. In these simulations, each robot uses $R_{ZOR} = 40$ meters, $R_{ZOO} = 274$ meters and $R_{ZOA} = 40$ meters. We gradually increase the number of robots from 10 to 50, and let the swarms move to a destination about 5 kilometers away. We test the presented navigation algorithm in different configurations using leader percentage 15%, 20% and 25% coupled with moving speed 3 MPS, 6 MPS and 9 MPS. Figure 5 shows the average arrival ratio. As we can see, when the moving speed is low (3 MPS), the average arrival ratio is 100%. Such results remain stable when the number of robots increases except for the cases of large swarms containing 50 robots and 15% or 20% leaders. However, when the moving speed is high (6 MPS and 9 MPS), the average arrival ratio drops significantly when the number of robots is over a threshold number (40 when the moving speed is 6 MPS; 35 when the moving speed is 9 MPS). We also notice that the increase of leader percentage can effectively improve the average arrival ratio of large robot swarms. Figure 6 shows the average arrival time. We observe that the more robots a swarm has, the more time the swarm requires to arrive at the destination. We also notice that once the number of robots increases beyond a threshold number when moving at 6 MPS or 9 MPS, the average arrival time increases sharply. This is because when the moving speed is high, it takes much more time for large robot swarms to coordinate and make consensus decisions on the moving direction. Finally, when the moving speed is low, the different leader percentage would not improve the average arrival time; however, when the moving speed is high, more leaders could effectively reduce the average arrival time of large robot swarms.

C. Evaluation of the Percentage of Leaders

The percentage of leaders in the robot swarms is certainly an important parameter in the presented navigation algorithm. In the third set of simulations, we set the destination point to be 5 kilometers away, and let each robot use $R_{ZOR} = 40$ meters, $R_{ZOO} = 274$ meters and $R_{ZOA} = 40$ meters. Then we gradually increase the percentage of leaders from 10% to 25% to evaluate the performance of the navigation algorithm in robot swarms containing 10, 20, 30, 40, 50 robots and moving at the speed of 3 MPS, 6 MPS and 9 MPS. Figure 7 shows the average arrival ratio. For small swarms containing 30 or less robots, the arrival ratio is always 100%, and such result remain stable with different leader percentage or moving speed; For large swarms containing 40 or more robots, the average arrival ratio is low initially. However, it can be effectively improved with increase of leader percentage, especially when each robot moves at a high speed of 6 MPS or 9 MPS. Figure 8 shows the corresponding average arrival time of Figure 7. In general, the faster the robots move, the quicker robot swarms arrive at the destination. However, we observe fluctuations for the robot swarm containing 50 robots, for these particular robot swarms, their average arrival time is unstable when the moving speed is 9 MPS, since the average arrival ratio is very low.

D. Evaluation of the Moving Speed

Finally, we evaluate the presented navigation algorithm using different moving speed. In these simulations, each robot uses $R_{ZOR} = 40$ meters, $R_{ZOO} = 274$ meters and $R_{ZOA} = 40$ meters. We gradually increase the moving speed from 1 MPS to 10 MPS, and compare the performance of our algorithm in robot swarms containing 10, 20, 30, 40 and 50 robots, and having 15%, 20% and 25% leaders. Again, the destination point is about 5 kilometers away. Figure 9 shows the average arrival ratio of the robot swarms. For small swarms containing 30 or less robots, the average arrival ratios remain stable when the moving speed increases. However, for large swarms with 40 or more robots, the increase of moving speed can significantly degrade the average arrival ratio when the leader percentage is low. We also observe that this negative effect can be effectively improved if the leader percentage increases. Figure 10 shows the average arrival time of the robot swarms. In general, the more robots a swarm has, the more time the swarm needs to arrive at the destination. Furthermore, the increase of leader percentage would not improve the average arrival time.

E. Summary of Simulation Results

The key results of the all of the simulations can be summarized as follows. (1)When using proper configurations, the presented navigation algorithm can effectively lead the robot swarms to the destination. Such results remain stable within a wide range of swarm size, moving speed and leader percentage. (2) For large robot swarms containing 40 or more robots, the successful arrival ratio drops when the moving speed is high or the leader percentage is low. This implies that for a given
Fig. 3. The hollow circles stand for the non-leader robots, while the solid circles stand for the leader robots. The dot-line crossing in the up-right corner is the destination. (a) The initial topology of the wireless robot swarm. (b) The topology of the wireless robot swarm at 800 seconds. (c) The topology of the wireless robot swarm at 1500 seconds.

Fig. 4. Average arrival ratio and arrival time of a robot group containing 30 robots with 15% leaders moving to a destination point about 5 kilometers away. (a) Average arrival ratio. (b) Average arrival time.

Fig. 5. Average arrival ratio of the wireless robot swarms containing 15%, 20% and 25% leaders and moving at the speed of 3 MPS, 6 MPS and 9 MPS, respectively. (a) Moving Speed = 3 MPS. (b) Moving Speed = 6 MPS. (c) Moving Speed = 9 MPS.
robot swarm where each robot uses fixed radii of ZOR, ZOO and ZOA, there is a threshold moving speed and a threshold leader percentage in the presented algorithm. In order to achieve better performance, the moving speed must be lower than the threshold value or the leader percentage must be higher than the threshold value. This points out an important future research issue: to derive the thresholds of moving speed and leader percentage using mathematical analysis.

V. Conclusion and Future Work

This paper presents an autonomous navigation algorithm for wireless robot swarms. Unlike traditional navigation problems and solutions, our model aims to navigate robot swarms using covert leaders where only a small number of leader robots possess the destination information, and both the leaders’ identities and the destination information should remain secret at all time. Our model is fully distributed and robots coordinate via wireless communications without any synchronization. Simulation results show that through local coordinations, covert leaders can effectively help robot swarms make a consensus.
decision on moving direction and thus lead the robot swarms to successfully arrive at the destination. Future research includes mathematically analyzing the thresholds of moving speed and leader percentage for the given configuration of robot swarms, as well as extending our algorithm to more complicated scenarios, such as each robot has kinetic constraints and static or mobile obstacles exist in the environment.

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