

```

% Data Fitting by Least Squares (polynomials)
% Input : x=(x1,...xm)' - x coordinations of data
%         y=(y1,...,ym)' - y coordination of data
% Output: p=(p1,...,pn-1): P(x)=p1+p2x+...pn-1x^(n-2) - the best polynomial
% degree n-2 and plot of the set of data and y=P(x).

```

```
function [p]=LeastS(x,y,n)
```

```
m=length(x);
```

```
for k=1:m
```

```
    A(k,1)=1;
```

```
    for j=2:n-1
```

```
        A(k,j)=x(k)^(j-1);
```

```
    end
```

```
end
```

```
%Solving the normal equation
```

```
p=(A'*A)\(A'*y)
```

```
%Plotting
```

```
for s=1:n-1;
```

```
    c(s)=p(n-s);
```

```
end
```

```
a=x(1)-1;
```

```
b=x(m)+1;
```

```
w=a:0.05:b;
```

```
pw=polyval(c,w);
```

```
plot(x,y,'o',w,pw)
```

```
grid
```

```
% Calculating RMSE
```

```
RMSE=0;
```

```
for k=1:m
```

```
    RMSE=RMSE+(polyval(c,x(k))-y(k))^2;
```

```
end
```

```
RMSE=sqrt(RMSE/m)
```

```
% Similar to polyfit MatLab default command.
```

---

```
% Set of data: (3,3), (-1,2), (0,1), (1,-1), (3,4).
```

```
% Model: y=p1+p2x+p3x^2
```

```
clear;
```

```
x=[-3;-1;0;1;3];
```

```
y=[3;2;1;-1;-4];
```

```
n=4;
```

```
p=LeastS(x,y,n)
```

```
p =
```

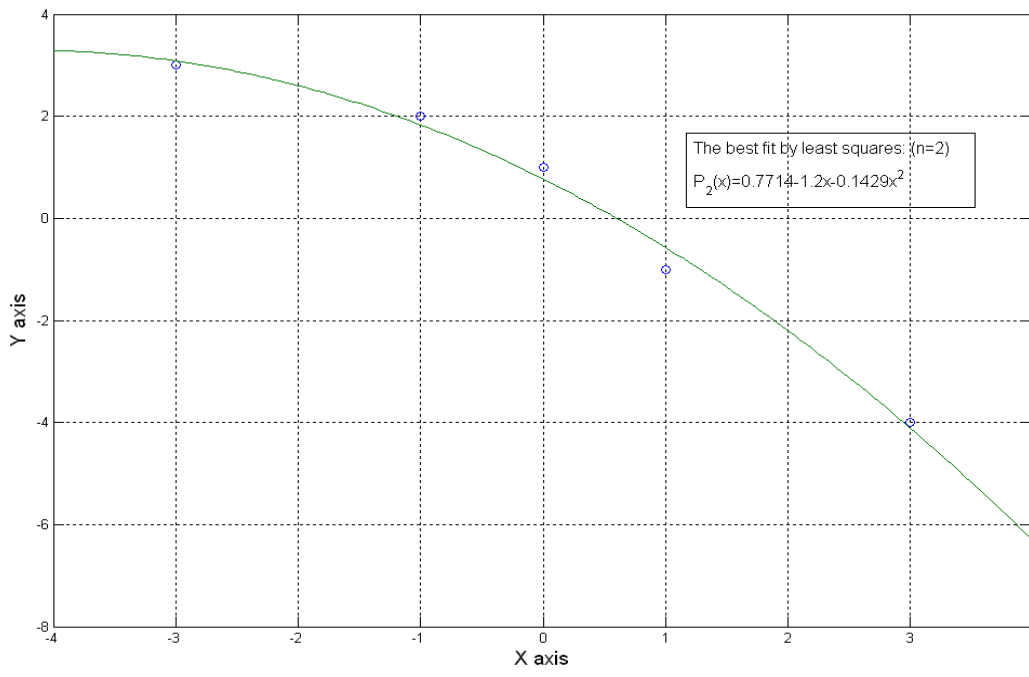
```
    0.7714
```

```
   -1.2000
```

```
   -0.1429
```

```
RMSE =
```

```
    0.2390
```




---

```
% Model: y=p1+p2x+p3x^2+p4x^3+p4x^4- produces interpolation
```

```
n=6;
```

```
p=LeastS(x,y,n)
```

```
p =
```

```
1.0000
```

```
-1.5417
```

```
-0.5417
```

```
0.0417
```

```
0.0417
```

```
RMSE =
```

```
5.9829e-015
```

